

1.6 Inverse Functions

Review of Inverses you already know:

1) Additive Inverse:

- What is the additive inverse of 2?
- What do you get when you combine additive inverses?
- What is the **identity element** for **addition**?

(Identity element gives back what you put in)

2) Multiplicative Inverse:

- What is the multiplicative inverse of 2?
- What do you get when you combine multiplicative inverses?
- What is the **identity element** for **multiplication**?

(Identity element gives back what you put in)

INVERSES “UNDO” ONE ANOTHER

3) **Composition** is an “operation” unique to functions.

Ex: $f(x) = x+3$, what function, $g(x)$ would “undo” $f(x)$?

$g(x) =$ _____

What is $f(g(x))$? _____ $g(f(x))$ _____

What is the **identity function**? _____

If $f(g(x))=x$ and $g(f(x))=x$ then f and g are inverses of one another.

$$g(x) = f^{-1}(x) \quad \underline{\text{read as the inverse of } f}$$

$$f(x) = x+3 \qquad f^{-1}(x) = x-3$$

x	1	2	3	0	-1
f(x)	4	5	6	3	2

x	4	5	6	3	2
$f^{-1}(x)$	1	2	3	0	-1

What do you notice?

Property of Inverses: the domain of $f =$ _____ of f^{-1}
 The range of $f =$ _____ of f^{-1}

To verify inverses algebraically – show that
 _____ = x and $g(f(x)) =$ _____

Example: Show that $f(x) = \frac{x-9}{4}$ and $g(x) = 4x + 9$

are inverses of one another.

Additional practice p.69 #9-14

Put the equations of two inverses into your graphing calculator as y_1 and y_2 . Zoom 5 (Zoom Square)

Is there a line of symmetry between these two graphs?

What is its equation?

Additional practice p69 #15-24

Verifying functions – Graphically and Numerically

If $y = x$ is a line of symmetry then $f(x)$ and $g(x)$ are inverses. Be sure to look at them in zoom square mode.

To verify inverses numerically – use the table feature of the graphing calculator.

Input $f(x)$ in y_1 and $g(x)$ in y_2

$y_3 = y_1(y_2)$ and $y_4 = y_2(y_1)$

If the values of x , y_3 and y_4 are all the same then f and g are inverses.

Practice p 70 #25-28

For a function to have an inverse function, it must be a **one-to-one** function. Every x and every y is unique.

Passes both **vertical line test** and **Horizontal line test**.

Practice p 70 #28-40

Finding an Inverse **ALGEBRAICALLY:**

- 1) **Replace $f(x)$ with y .**
- 2) **Change x to y and y to x .**
- 3) **Get all the y 's on one side and everything else on the other side of the equation**
- 4) **Solve for y (may have to factor out y)**

Ex1 $f(x) = 3x + 5$ find its inverse function, if it exists

- 1) **Graph $f(x)$ to see if it is a One-to-One function. What is the test used?**
- 2) **Go through the steps above if it passes the test in #1.**
- 3) **Verify inverses algebraically or graphically.**

Ex 2 $f(x) = \frac{2x + 3}{3x - 5}$

Ex 3 $f(x) = x^3 - 5$

Additional practice: p70 # 41-62

Given graph of function – to find its inverse **Swap the domain and range values.**

P70 #67-68

Additional practice on inverses and composition: p71 #73-82